

Chapter 17: Probability Models

Bermouli Trials:

- Two possible outcomes~ success/ failure
- Probability, p, is constant for each trial
- Each trial is independent

*To test a Bermouli trial you can use a Geometric model, a Binomial model or a Normal model

Geometric Model:

~ one parameter, p, (probability of success) represented by Geom(p)

P = success q: (p-1)=failure x= # of trials

$P(X=x) = qx-1p$ expected value: $\mu=1/p$

Standard deviation: $\sigma = \sqrt{q/p^2}$

*consider the 10% condition: sample is smaller than 10% of the population

Ex: The American Red Cross says that about 11% of the U.S. population has Type B blood. A blood drive is being held in your area. What is the probability that the fourth blood donor is the first donor with Type B blood?

$$p(4) = q^{4-1} \times p = (.89)^{4-1} (.11) = .89^3 \times .11 = .0775$$

Binomial Model:

~ two parameters, Binom(n,p)

Probability of k success in n trials is: b(n,k,p)

$$(x + a)^n = \sum_{k=0}^n \binom{n}{k} x^k a^{n-k}$$

Mean: $\mu=np$ standard deviation: $\sigma = \sqrt{npq}$

-a binomial model describes the number of successes in a specified number of trials two parameters= # of trials, probability of success, p,

*still check 10% condition

* success/failure condition: at least 10 successes and 10 failures

Ex: only 6% of people have o-negative blood. Suppose 20 donors come to the blood drive. What is the probability that there are 2 or 3 universal donors?

$$P(X=2 \text{ or } 3) = P(X=2) + P(X=3)$$

$$\binom{20}{2} (.06)^2 (.94)^{18} + \binom{20}{3} (.06)^3 (.94)^{17} \sim .2246 + .0860 = .3106$$